

251.01

(1) $\vec{r}_1 = -1\hat{x} + 2\hat{y}$

$\vec{r}_2 = 1\hat{x} + 2\hat{y}$

$\vec{r}_3 = 0\hat{x} + 0\hat{y}$

$\vec{r}_p = 5\hat{x} + 4\hat{y}$

$\vec{r}_{1p} = \vec{r}_p - \vec{r}_1 = (5 - (-1))\hat{x} + (4 - 2)\hat{y}$
 $= 6\hat{x} + 2\hat{y}$

$\vec{r}_{2p} = \vec{r}_p - \vec{r}_2 = (5 - 1)\hat{x} + (4 - 2)\hat{y}$
 $= 4\hat{x} + 2\hat{y}$

$\vec{r}_{3p} = \vec{r}_p - \vec{r}_3 = (5 - 0)\hat{x} + (4 - 0)\hat{y}$
 $= 5\hat{x} + 4\hat{y}$

$$\vec{r}_{3p} = \vec{r}_p - \vec{r}_3 = (5-0)\hat{x} + (4-0)\hat{y} = 5\hat{x} + 4\hat{y}$$

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example: $\hat{r}_{ip} = \frac{\vec{r}_{ip}}{|\vec{r}_{ip}|} = \frac{6\hat{x} + 2\hat{y}}{\sqrt{36+4}}$
 $= \frac{6\hat{x}}{6.3} + \frac{2\hat{y}}{6.3} = 0.95\hat{x} + 0.32\hat{y}$

$$\vec{E}_p = k\mu \left[(+1) \frac{6\hat{x} + 2\hat{y}}{[6^2 + 2^2]^{3/2}} + (-2) \frac{4\hat{x} + 2\hat{y}}{[4^2 + 2^2]^{3/2}} + (+4) \frac{5\hat{x} + 4\hat{y}}{[5^2 + 4^2]^{3/2}} \right]$$

$$\left[\frac{\hat{r}_{ip}}{r_{ip}^2} \right] = \frac{\vec{r}_{ip}}{(r_{ip}^2)^{3/2}}$$

$$[-1^2 + 5^2] = -1 \times 25 = 26$$

$$\vec{r}_p = \vec{r}_p - \vec{r}_3 = (5-1)\hat{x} + (4-2)\hat{y} = 4\hat{x} + 2\hat{y}$$

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$$\vec{E}_p = k\mu \left[(+1) \frac{6\hat{x} + 2\hat{y}}{[6^2 + 2^2]^{3/2}} \right] \leftarrow$$

$$\left[\frac{\hat{r}_{ip}}{r_{ip}^2} \right] + (-2) \frac{4\hat{x} + 2\hat{y}}{[4^2 + 2^2]^{3/2}} + (+4) \frac{5\hat{x} + 4\hat{y}}{[5^2 + 4^2]^{3/2}}$$

$$[-1^2 + 5^2] = -1 \times 25 = 26$$

$$V_p = \sum_{i=1}^n k \frac{q_i}{|\vec{r}_{ip}|}$$

$$= k \mu \left[\frac{(+1)}{\sqrt{6^2 + 2^2}} + \frac{(-2)}{\sqrt{4^2 + 2^2}} + \frac{(+4)}{\sqrt{5^2 + 4^2}} \right]$$

1. 2.
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$$W_1 = 0$$

$$W_2 = q_2 V_{at 2} \text{ from 1}$$

$$W_3 = q_3 V_{at 3} \text{ from 1} + q_3 V_{at 3} \text{ from 2}$$

$$\begin{aligned} \vec{r}_{12} &= \vec{r}_2 - \vec{r}_1 = \\ &= (\hat{x} + 2\hat{y}) - (-\hat{x} + 2\hat{y}) \\ &= 2\hat{x} \end{aligned}$$

$$V_{at2} = R\mu \cdot \frac{(+1)}{2}$$

from 1

$$W_2 = R\mu \frac{(+1)}{2} \cdot (-2\mu)$$

$$V_{at3} = \vec{r}_{13} = \vec{r}_3 - \vec{r}_1 = -\hat{x} + 2\hat{y}$$

from 1

$$|\vec{r}_{13}| = \sqrt{1^2 + 2^2} = \sqrt{5}$$

$= 2.24$

$$|\vec{r}_{23}| = |-\hat{x} - 2\hat{y}| = 2.4$$

$$V_{g3} = \vec{r}_3 - \vec{r}_1 = -1\hat{x} + 2\hat{y}$$

$$|\vec{r}_{13}| = \sqrt{1^2 + 2^2} = \sqrt{5}$$

$$|\vec{r}_{23}| = |-1\hat{x} - 2\hat{y}| = 2.4$$

$$W = 0$$

$$+ -2\mu\mu k \left(\frac{1}{2}\right)$$

$$+ 4\mu\mu k \left[\left(\frac{(+1)}{2.4}\right) + \left(\frac{(-2)}{2.4}\right) \right]$$

$$W \cdot [J]$$

$$V \left[\frac{J}{C} \right] V.$$

$$E \left[\frac{N}{C} \right] \left[\frac{V}{m} \right] \left[\frac{J}{mC} \right]$$

$$V = ax + by + c$$

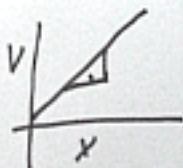
$$V = ax + by + c$$

~~$$V = ax + by + c$$~~

$$\vec{E} = - \frac{\partial V}{\partial x} \hat{x} = -a \hat{x}$$

$$\vec{E} = - \frac{\partial V}{\partial x} \hat{x} - \frac{\partial V}{\partial y} \hat{y}$$

$$= -a \hat{x} - b \hat{y}$$



$$V = ax^2 + by^2 \quad 2$$

$$\vec{E} = -\vec{\nabla} V = - \left[\frac{\partial V}{\partial x} \hat{x} + \frac{\partial V}{\partial y} \hat{y} \right]$$

$$= - \left[2ax \hat{x} + 2by \hat{y} \right]$$

#3:220



$$\rho(\vec{r}) = \frac{Q}{\frac{4}{3}\pi a^3}$$

$$\Phi_E = \frac{Q_{enc}}{\epsilon_0}$$

outside $Q_{enc} = \rho V_{sphere}$

$$= \frac{Q}{\frac{4}{3}\pi a^3} \left(\frac{4}{3}\pi a^3 \right)$$

$$= Q$$

$$\Phi_E = \sum_{\Delta A_i} \vec{E}_i \cdot \Delta \vec{A}_i = \sum_{\Delta A_i} E_i \Delta A_i$$

$$= E \sum_{\Delta A_i} \Delta A_i = E(4\pi r^2)$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0} \Rightarrow \vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$

$$\frac{4}{3}\pi a^3$$

$$= Q$$

$$\Phi_E = \sum_{\Delta A_i} \vec{E}_i \cdot \Delta \vec{A}_i = \sum_{\Delta A_i} E_i \Delta A_i$$

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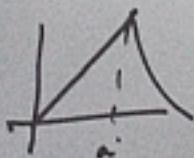
$$E(4\pi r^2) = \frac{Q}{\epsilon_0} \Rightarrow \vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$



$r \leq a$
 $\vec{E} \parallel \vec{A}$
 E uniform

$$Q_{enc} = \rho \cdot V_G$$

$$= \frac{Q}{\frac{4}{3}\pi a^3} \left(\frac{4}{3}\pi r^3 \right)$$



$$Q_{enc} = Q \left(\frac{r}{a} \right)^3$$

$$\Phi_E = (E \cdot 4\pi r^2)$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0} \left(\frac{r}{a} \right)^3$$

$$\vec{E} = \frac{Q}{\epsilon_0 a^3} \cdot \frac{1}{4\pi} \hat{r}$$

$$\rho = \rho_0 \frac{r}{a}$$

$$Q = 4\pi \int_0^a \rho_0 \frac{r}{a} \cdot r^2 dr$$

$$= \frac{4\pi}{a} \rho_0 \int_0^a r^3 dr$$

$$= \frac{4\pi}{a} \rho_0 \frac{r^4}{4} \Big|_0^a = \pi \rho_0 a^3$$

$$\rho_0 = \frac{Q}{\pi a^3}$$

$$a \rightarrow \frac{1}{4} \rightarrow 10^{-}$$

$$\rho_0 = \frac{Q}{\pi a^3}$$



$$\rho = \rho_0 \frac{r}{a}$$

$$\phi_E = \frac{Q_{enc}}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{A} = \oint E \cdot dA$$

$$= \oint E dA = E \oint dA$$

$$= E(4\pi r^2)$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0 r^2} Q; \rho_0 = \frac{Q}{\pi a^3}$$

$$a \rightarrow \frac{1}{4} \rightarrow 10^{-}$$

$$\rho_0 = \frac{Q}{\pi a^3}$$



$$\rho = \rho_0 \frac{r}{a}$$

$$\phi_E = \frac{Q_{enc}}{\epsilon_0}$$

$$\vec{E} \parallel \vec{A}$$

$$|\vec{E}| \text{ const}$$

$$\oint \vec{E} \cdot d\vec{A}$$

$$= \oint E dA = E \oint dA$$

$$= E(4\pi r^2)$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0 r^2} Q; \rho_0 = \frac{Q}{\pi a^3}$$



On GS:

$\vec{E} \parallel \vec{A}$

$|\vec{E}|$ uniform

$$Q_{enc} = 4\pi \int_0^r \rho_0 \frac{r}{a} \cdot r^2 dr$$

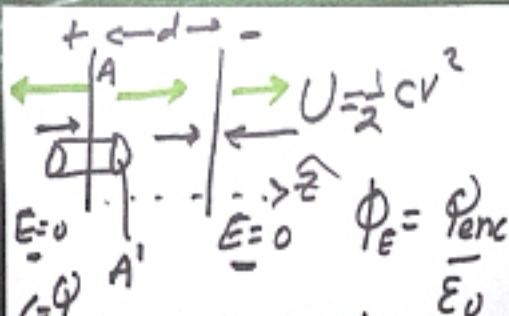
$$= 4\pi \rho_0 \int_0^r r^3 dr$$

$$= \frac{4\pi \rho_0}{a} \frac{r^4}{4}$$

$$\phi_E = \oint \vec{E} \cdot d\vec{A} = \oint E dA = E \oint dA$$

$$\phi_E = E(4\pi r^2)$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{\pi \rho_0 r^4}{r^2} \cdot \frac{1}{r}, \rho_0 = \frac{Q}{\pi a^3}$$



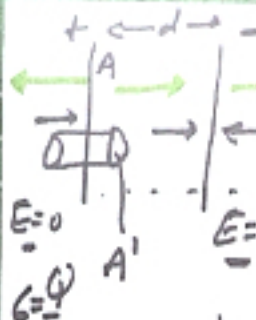
$$\phi_E = \underline{EA'} \quad \phi_{enc} = \underline{QA'}$$

$$\vec{E} = \frac{\vec{E}}{\epsilon_0} \hat{z} \quad \therefore EA' = \frac{QA'}{\epsilon_0} \Rightarrow \vec{E} = \frac{\epsilon_0}{\epsilon_0} \hat{z}$$

$$\vec{E} = -\frac{\delta V}{\delta x} \hat{z} \quad V = -Ed \quad \left(E = -\frac{\delta V}{\delta x} = -\frac{\delta V}{d} \right)$$

$$C = \left| \frac{Q}{V} \right| = \frac{QA}{\frac{\epsilon_0}{\epsilon_0} d} = \underline{\underline{\epsilon_0 \frac{A}{d}}}$$

So:

$+ \leftarrow d \rightarrow -$

 $U = \frac{1}{2} CV^2$
 $E = 0$

$$\Phi_E = \frac{Q}{\epsilon_0} \quad \Phi_E = \frac{Q_{enc}}{\epsilon_0}$$

$$\vec{E} = \frac{\sigma}{\epsilon_0} \hat{z} \quad \therefore EA' = \frac{\sigma A'}{\epsilon_0} \Rightarrow \vec{E} = \frac{\sigma}{\epsilon_0} \hat{z}$$

$$\vec{E} = -\frac{\partial V}{\partial x} \quad V = -Ed \quad \left(E = -\frac{\partial V}{\partial x} = -\frac{\partial V}{d} \right)$$

$$C = \frac{Q}{V} = \frac{\sigma A}{\frac{\sigma d}{\epsilon_0}} = \underline{\underline{\epsilon_0 \frac{A}{d}}}$$

So:

$$C = K C_{geo} = 200 \times 8.8 \mu f$$

$$= 17.6 \times 10^{-4} f \quad 10^{-6}$$

$$C_1 = ~~1760~~ 1760 \mu f \quad C_1 \quad C_2$$

$$C_2 = 1760 \mu f \quad \text{---|---|---}$$

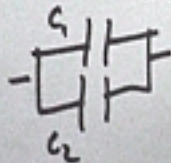
Series: $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$

$$= \frac{2}{1760} \Rightarrow C = \frac{1760}{2}$$

Series: $= 8.8 \mu f$

Parallel: $C = C_1 + C_2 = 3520 \mu f$

$$3.5 \times 10^{-3} f$$



$$\epsilon_0 = 8.854 \times 10^{-12}$$

$$\begin{aligned} C_{\text{geo}} &= 8.854 \left(\frac{1000 \text{ m}^2}{1 \times 10^{-3} \text{ m}} \right) \times 10^{-12} \\ &= 8.854 \times 10^{-12} (1 \times 10^3 \times 10^3) \\ &= 8.854 \times 10^{-6} \text{ F} = \underline{8.854 \mu\text{F}} \end{aligned}$$

$$\begin{aligned} U: E &= \frac{V}{d} = \frac{100 \text{ V}}{1 \times 10^{-3} \text{ m}} \quad (U_E = \frac{1}{2} \epsilon_0 E^2) \\ &= 1 \times 10^2 \times 10^3 = 1 \times 10^5 \frac{\text{V}}{\text{m}} \end{aligned}$$

$$\begin{aligned} U &= \frac{1}{2} C V^2 = \frac{1}{2} \times 8.854 \times 10^{-6} (100)^2 \\ &= 4.4 \times 10^{-6} \times 1 \times 10^4 \\ &= 4.4 \times 10^{-2} \text{ J} \end{aligned}$$

U₀₁

$$\epsilon_0 = 8.854 \times 10^{-12}$$

$$\begin{aligned} C_{\text{geo}} &= 8.854 \left(\frac{1000 \text{ m}^2}{1 \times 10^{-3} \text{ m}} \right) \times 10^{-12} \\ &= 8.854 \times 10^{-12} (1 \times 10^3 \times 10^3) \\ &= 8.854 \times 10^{-6} \text{ f} = \underline{8.854 \mu\text{F}} \end{aligned}$$

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$$\begin{aligned} U &= \frac{1}{2} C V^2 = \cancel{4.42} \times 10^{-6} (100)^2 \\ &= 4.4 \times 10^{-6} \times 1 \times 10^4 \\ &= 4.4 \times 10^{-2} \text{ J} \end{aligned}$$

U₀₁

$$R_1 = 100\Omega \quad R_2 = 300\Omega$$

$$R_{\text{series}}: \text{---} \overset{R_1}{\text{M}} \text{---} \overset{R_2}{\text{M}} \text{---}$$

$$R_1 + R_2 = 400\Omega$$

$$R_{\text{par}}: \begin{array}{c} \text{---} \overset{R_1}{\text{M}} \text{---} \\ | \\ \text{---} \underset{R_2}{\text{M}} \text{---} \end{array} = \frac{1}{\frac{1}{R} + \frac{1}{R_1} + \frac{1}{R_2}}$$

$$\frac{1}{R} = \frac{1}{300} + \frac{1}{100} \Rightarrow$$

$$: R_{||} = 75\Omega$$

$$\frac{R_{\text{ser}}}{R_{\text{par}}} = \frac{400}{75} = 5.33$$

$$R_1 = 100\Omega \quad R_2 = 300\Omega$$

$$R_{\text{series}}: \text{---} \overset{R_1}{\text{M}} \text{---} \overset{R_2}{\text{M}} \text{---}$$

$$R_1 + R_2 = 400\Omega$$

$$R_{\text{par}}: \begin{array}{c} \text{---} \overset{R_1}{\text{M}} \text{---} \\ | \\ \text{---} \overset{R_2}{\text{M}} \text{---} \end{array} \text{---} \frac{1}{\frac{1}{R} + \frac{1}{R_1} + \frac{1}{R_2}}$$

$$\frac{1}{R} = \frac{1}{300} + \frac{1}{100} \Rightarrow$$

$$: R_{||} = 75\Omega$$

$$\frac{R_{\text{ser}}}{R_{\text{par}}} = \frac{400}{75} = 5.33$$


 $V = k \frac{q}{r} \rightarrow V = k \frac{Q}{a}$

$$C = \frac{Q}{V} = \frac{Q}{kQ/a} = \frac{a}{k}$$



$$S = r \text{ radially}$$

$$\Phi_E = \sum_{\Delta A_i} \vec{E}_i \cdot \vec{\Delta A}_i$$

$$= E(2\pi sh)$$

$$\Phi_{\text{enc}} = \oint \vec{E} \cdot d\vec{A}$$

$$= E(2\pi sh)$$

$$Q_{\text{enc}} = \lambda h$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 S} \hat{s}$$

$$\frac{\lambda \ell}{h} \oint \vec{E} \cdot d\vec{A} = \oint \vec{E} \cdot d\vec{A} \\ = E(2\pi sh)$$

$$\Delta V = \sum \vec{E} \cdot \Delta \vec{S}$$

$$= \int \vec{E} \cdot d\vec{S}$$

$$= \sum \frac{\lambda}{2\pi\epsilon_0 s} \Delta s = \frac{\lambda}{2\pi\epsilon_0} \sum \frac{\Delta s}{s}$$

$$= \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

$$\Delta V = \int_a^b \frac{\lambda}{2\pi\epsilon_0 s} ds = \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

$$C = \frac{Q}{V} = \frac{\lambda h}{\frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)}$$



$$S = \text{radius}$$

$$\oint \vec{E} \cdot d\vec{A} = \sum \vec{E}_i \cdot \Delta \vec{A}_i$$

$$= E(2\pi sh)$$

$$\cancel{Q_{\text{enc}}} = \oint \vec{E} \cdot d\vec{A}$$

$$= E(2\pi sh)$$

$$Q_{\text{enc}} = \lambda h$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 S} \hat{s}$$

$$Q_{enc} = \oint \vec{E} \cdot d\vec{A} = E(2\pi sh)$$

$$Q_{enc} = \lambda h$$

$$\vec{E} = \frac{\lambda}{2\pi\epsilon_0 s} \hat{s}$$

$$\Delta V = \sum \vec{E} \cdot \Delta \vec{s}$$

$$= \int \vec{E} \cdot d\vec{s}$$

$$= \sum \frac{\lambda}{2\pi\epsilon_0 s} \Delta s = \frac{\lambda}{2\pi\epsilon_0} \sum \frac{\Delta s}{s}$$

$$= \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

$$\Delta V = \int_a^b \frac{\lambda}{2\pi\epsilon_0 s} ds = \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

$$C = \frac{Q}{V} = \frac{\lambda h}{\frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)}$$

$$\frac{2\pi\epsilon_0}{h} = \frac{1}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

Qenc $\Delta V = \int_a^b \frac{1}{2\pi\epsilon_0} \frac{ds}{s} = \frac{1}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$

E. $C = \frac{Q}{V} = \frac{2\pi\epsilon_0 h}{\ln\left(\frac{b}{a}\right)}$

$$U = \frac{1}{2} C V^2$$

$$= \frac{1}{2} \frac{2\pi\epsilon_0 h}{\ln\left(\frac{b}{a}\right)} \cdot \left[\frac{1}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right) \right]^2$$

$$= \frac{1}{2} \frac{h}{\ln\left(\frac{b}{a}\right)} \cdot \frac{1}{2\pi\epsilon_0} \cdot \ln^2\left(\frac{b}{a}\right)$$

$$U = \frac{1}{2} C V^2 \quad U_E = \frac{1}{2} \epsilon_0 E^2$$