



$$1 = \left(\frac{1}{2}\right)^2 + y^2$$

$$\Rightarrow y^2 = 1 - \frac{1}{4} = \frac{3}{4}$$

$$y = \frac{\sqrt{3}}{2} = 0.866$$

$$y_p = \frac{1}{2}y = 0.433$$

$$\vec{E}_p = k \sum_{i=1}^3 \frac{q_i}{r_{ip}^2} \vec{r}_{ip}$$

$$\vec{r}_1 = -\frac{1}{2}\hat{x} + 0\hat{y} \quad \vec{r}_2 = \frac{1}{2}\hat{x} + 0\hat{y}$$

$$\vec{r}_3 = 0\hat{x} + 0.866\hat{y}$$

$$\vec{r}_p = 0\hat{x} + 0.433\hat{y}$$

$$\vec{r}_p = 0\hat{x} + .433\hat{y}$$

$$\vec{r}_{1p} = \vec{r}_p - \vec{r}_1 = (0\hat{x} - \frac{1}{2}\hat{x}) + .433\hat{y}$$

$$\vec{r}_{2p} = \vec{r}_p - \vec{r}_2 = (0 - \frac{1}{2})\hat{x} + .433\hat{y}$$

$$\vec{r}_{3p} = \vec{r}_p - \vec{r}_3 = (0 - 0)\hat{x} + (-.866)\hat{y}$$

$$\vec{r}_{1p} = .5\hat{x} + .433\hat{y}$$

$$\vec{r}_{2p} = -.5\hat{x} + .433\hat{y}$$

$$\vec{r}_{3p} = 0\hat{x} - .866\hat{y}$$

$$\begin{aligned}\vec{r}_{3p} &= (0\hat{x} + .433\hat{y}) - (0\hat{x} + .866\hat{y}) \\ &= 0\hat{x} - .433\hat{y}\end{aligned}$$

$$\vec{E}_p = kM \left[(+) \frac{.5\hat{x} + .433\hat{y}}{[.5^2 + .433^2]^{3/2}} \right.$$

$$+ (+) \frac{-.5\hat{x} + .433\hat{y}}{[.289]}$$

$$+ (+) \frac{0\hat{x} - .433\hat{y}}{[0^2 + (.433)^2]^{3/2}} \Big]$$



$$\vec{E}_p = kM \left[\frac{(.433 \times 2)\hat{y}}{.289} - \frac{.433\hat{y}}{(.433)^3} \right]$$

$$= kM \left[\frac{.866}{.289} - 5.33 \right] \hat{y}$$

$$+ (+) \frac{-5\hat{x} + .433\hat{y}}{[.289]}$$

$$+ (+) \frac{0\hat{x} - .433\hat{y}}{[0^2 + (.433)^2]^{3/2}}$$



$$\left| \begin{aligned} \vec{E}_p &= kM \left[\frac{(.433 \times 2)\hat{y}}{.289} - \frac{.433\hat{y}}{(.433)^3} \right] \\ &= kM \left[\frac{.866}{.289} - 5.33 \right] \hat{y} \end{aligned} \right.$$

$$^y = kM [2.99 - 5.33] \hat{y}$$

$$= kM [-2.34] \hat{y}$$

$$= -2.34 (8990) \hat{y}$$

$$= -21010 \hat{y}$$

$$= -2.1 \times 10^4 \hat{y} \frac{N}{C}$$



$$\vec{r}_{ip} = x\hat{x} + y\hat{y}$$

$$\frac{\vec{r}_{ip}}{|\vec{r}_{ip}|^{3/2}} = \frac{x\hat{x} + y\hat{y}}{[x^2 + y^2]^{3/2}}$$

$$\begin{aligned} \frac{\hat{r}_{ip}}{r_{ip}^2} &= \frac{x\hat{x} + y\hat{y}}{[x^2 + y^2]^{3/2}} \\ &= \frac{x\hat{x} + y\hat{y}}{[x^2 + y^2]^{3/2}} \end{aligned}$$



$$\vec{E}_p = k\mu \sum \frac{q_i \vec{r}_{ip}}{r_{ip}^3} \quad \frac{\vec{r}_{ip}}{|\vec{r}_{ip}|^2}$$

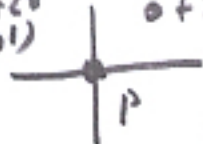
$$|\vec{r}_{ip}| = \sqrt{x^2 + y^2} \quad \vec{r}_{ip}$$

$$|\vec{r}_{ip}| = |\vec{r}_{ip}|^3 \frac{1}{[x^2 + y^2]^{3/2}}$$

① $+20$
 $(-1, 1)$

② $+20$
 $(1, 1)$

③



$$\vec{r}_1 = 1\hat{x} + 1\hat{y}$$

$$\vec{r}_2 = -1\hat{x} + 1\hat{y}$$

$$\vec{r}_p = 0\hat{x} + 0\hat{y}$$

$$\vec{r}_{1p} = \vec{r}_p - \vec{r}_1 = -1\hat{x} - 1\hat{y}$$

$$\vec{r}_{2p} = 1\hat{x} - 1\hat{y}$$

$$\vec{E}_p = 20\mu \left[\frac{-1\hat{x} - 1\hat{y}}{[1^2 + 1^2]^{3/2}} + \frac{1\hat{x} - 1\hat{y}}{[1^2 + 1^2]^{3/2}} \right]$$

$$\vec{r}_{21} = \hat{x} - \hat{y}$$

$$\vec{E}_p = 2k\mu \left[\frac{-\hat{x} - \hat{y}}{[1^2 + 1^2]^{3/2}} + \frac{\hat{x} - \hat{y}}{[1^2 + 1^2]^{3/2}} \right]$$

2.82

$$\vec{E}_p = \frac{2k\mu}{2.82} [-2\hat{y}]$$

$$= -\frac{4(8990)}{2.82} \hat{y}$$

$$= -(12751^2) \hat{y} \frac{N}{C}$$

$$= -1.275 \times 10^4 \hat{y} \frac{N}{C}$$



$$\vec{r}_1 = -\hat{x} + 0\hat{y} \quad \vec{r}_2 = 1\hat{x} + 0\hat{y}$$

$$\vec{r}_3 = 0\hat{x} + 1\hat{y} \quad \vec{r}_p = 0\hat{x} + 0\hat{y}$$

$$\vec{E}_p = k\mu \left[\frac{\hat{x} + 0\hat{y}}{[1^2 + 0^2]^{3/2}} + \frac{-\hat{x} + 0\hat{y}}{1} + \frac{0\hat{x} - 1\hat{y}}{1} \right]$$

$$\vec{E}_p = k\mu [2\hat{x} - 1\hat{y}]$$

$$= 17980\hat{x} - 8990\hat{y}$$

$$\vec{E}_p = 1.798 \times 10^4 \hat{x} - 8.99 \times 10^3 \hat{y} \frac{N}{C}$$

(9)
220-4



$$\rho = \frac{Q}{\frac{4}{3}\pi a^3} = \frac{3Q}{4\pi a^3}$$

outside



choose a GS

$$r > a$$

on GS: $\vec{E} \parallel \vec{A}$

$|\vec{E}|$ constant

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0} \quad \sum_{\substack{\Delta A_i \\ E \perp \Delta A_i}} \vec{E}_i \cdot \Delta \vec{A}_i = \frac{Q_{enc}}{\epsilon_0}$$

$$Q_{enc} = 0 \Rightarrow$$

$$\vec{E}_{out} = 0 \hat{r}$$

(4)
220-4



$$\rho = \frac{Q}{\frac{4}{3}\pi a^3} = \frac{3Q}{4\pi a^3}$$

outside



choose a GS

$$r > a$$

on GS: $\vec{E} \parallel \vec{A}$

$|\vec{E}|$ constant

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0} \quad \sum \vec{E}_i \cdot \Delta \vec{A}_i = \frac{Q_{enc}}{\epsilon_0}$$

$\vec{E} \cdot \Delta \vec{A}$ ΔA_i $E \Delta A_i$

$$Q_{enc} = 0 \Rightarrow$$

$$\vec{E}_{out} = 0 \hat{r}$$

$$E(4\pi r^2) = \frac{Q_{enc}}{\epsilon_0} \quad | \quad E(4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$\rho = \frac{3Q}{4\pi a^3}$$

$$\vec{E} = \frac{1}{\epsilon_0} \int \frac{3Q}{4\pi a^3} r^3 = \frac{Q}{4\pi \epsilon_0} \frac{1}{r^2} \hat{r}$$

+4.

$$Q_{enc} = \iiint \rho \cdot d^3r$$



Choose a GS
centered on charge
 $r \leq a$

Separate & superimpose
on GS: $\vec{E} \parallel \vec{A}$

$$|\vec{E}| = \text{const}$$

$$\oiint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$

$$\sum_i \vec{E} \cdot \Delta \vec{A}_i = \frac{Q_{enc}}{\epsilon_0}$$

$$\oiint E dA = \frac{Q_{enc}}{\epsilon_0}$$

$$\sum E_i \Delta A_i = \frac{Q_{enc}}{\epsilon_0}$$

$$E \oiint dA = \frac{Q_{enc}}{\epsilon_0}$$

$$E \sum \Delta A_i = \frac{Q_{enc}}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

+q:

$$\begin{aligned}
 Q_{\text{enc}} &= \iiint \rho \cdot d^3r \\
 &= 4\pi \int_0^r \rho \cdot r^2 dr \\
 &= 4\pi \rho \int_0^r r^2 dr \\
 &= \frac{4}{3} \pi \rho r^3
 \end{aligned}$$

$$Q_{\text{enc}} = \rho \cdot \frac{4}{3} \pi r^3$$

$$\vec{E}_{+q} = \frac{\rho \left(\frac{4}{3} \pi r^3 \right)}{\epsilon_0 (4\pi r^2)} \hat{r} = \frac{\rho r}{3\epsilon_0} \hat{r}$$

$$\vec{E}_{-q} = -\frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

superimposed

$$\vec{E} = \vec{E}_{+q} + \vec{E}_{-q} = \left[\frac{\rho}{3\epsilon_0} r - \frac{Q}{4\pi \epsilon_0 r^2} \right] \hat{r}$$

superimposed

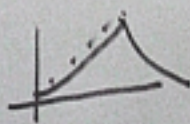
$$\vec{E} = \vec{E}_{+Q} + \vec{E}_{-Q} = \left[\frac{P}{3\epsilon_0} r - \frac{Q}{4\pi\epsilon_0 r^2} \right] \hat{r}$$

$$P = \frac{3Q}{4\pi a^3}$$

$$\vec{E} = \frac{1}{\epsilon_0} \left[\frac{3Q}{3(4\pi a^3)} r - \frac{Q}{4\pi r^2} \right] \hat{r}$$

$$= \frac{Q}{4\pi\epsilon_0} \left[\frac{r}{a^3} + \frac{1}{r^2} \right] \hat{r} \quad (r \leq a)$$

$$\frac{1}{a^2} - \frac{1}{a^2} = 0$$



250
4:

$$\rho = \rho_0 \frac{r}{a}$$



GS: $r > a$, centered

On GS: $|\vec{E}| = \text{const}$

$$\vec{E} \parallel \vec{r}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$Q_{\text{enc}} = \iiint \rho dV = 4\pi \rho_0 \int_0^a r^2 dr$$

$$= 4\pi \rho_0 \cdot \frac{a^3}{3} = \frac{4\pi \rho_0 a^3}{3}$$

$$\vec{E}_{\text{out}} = \frac{\rho_0 a^3}{\epsilon_0 (4\pi r^2)} \vec{r}$$

$$= \frac{\rho_0 a^3}{4\pi \epsilon_0 r^2} \vec{r}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$

$$E (4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$Q_{enc} = \iiint \rho dV = 4\pi \rho_0 \int_0^a r^2 dr$$

$$= \frac{4\pi \rho_0}{a} \cdot \frac{a^4}{4} = \pi \rho_0 a^3$$

$$\vec{E}_{out} = \frac{\pi \rho_0 a^3}{\epsilon_0 (4\pi r^2)} \hat{r}$$

$$= \frac{\rho_0 a^3}{4\epsilon_0 r^2} \hat{r}$$

inside



$$r \leq a$$

OnGS:

$|\vec{E}|$ uniform, $\vec{E} \parallel \vec{A}$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$Q_{enc} = \iiint \rho dV = \frac{4\pi \rho_0}{3\epsilon_0} \int_0^r r \cdot r^2 dr$$

$$= \frac{4\pi \rho_0}{3\epsilon_0} \cdot \frac{r^4}{4} = \frac{\pi \rho_0 r^4}{\epsilon_0 a}$$

1.2) Uniform, $\vec{E} \parallel \hat{r}$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$

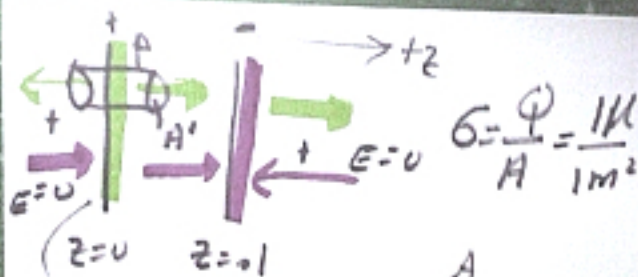
$$E(4\pi r^2) = \frac{Q_{enc}}{\epsilon_0}$$

$$\begin{aligned} Q_{enc} &= \iiint \rho dV = \frac{4\pi\rho_0}{a\epsilon_0} \int_0^r r \cdot r^2 dr \\ &= \frac{4\pi\rho_0}{a\epsilon_0} \cdot \frac{r^4}{4} = \frac{\pi\rho_0 r^4}{\epsilon_0 a} \end{aligned}$$

Inside:

$$\vec{E} = \frac{\pi\rho_0 r^4}{(4\pi r^2)a\epsilon_0} \hat{r}$$

$$\vec{E}_{in} = \frac{\rho_0 r^2}{4a\epsilon_0} \hat{r} \quad // \quad \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$$



$A = 1 \text{ m}^2$ On LSA: $\vec{\Phi} \rightarrow \vec{E}$

$$\vec{E} \cdot \vec{A} = 0$$

on ENds: $\vec{E} \cdot \vec{A} = EA'$

$$\vec{E} \cdot \vec{A} = EA'$$

$\vec{E} \parallel \vec{A}$, $|\vec{E}|$ uniform

$$\Phi_E = \frac{Q_{\text{enc}}}{\epsilon_0} \Rightarrow \Phi_E = EA'$$

$$Q_{\text{enc}} = CA'$$

$$\epsilon A' = \frac{QA'}{\epsilon_0} \Rightarrow \vec{E}_{in} = \frac{\sigma}{\epsilon_0} \hat{z}$$

$$\vec{E}_{out} = 0 \hat{z}$$

$$E = \frac{F}{q}$$

$$F = Eq$$

