

**Instructions: You have a total of 50 minutes to complete this test. Answer each of the following questions completely providing details and correct SI units.**

Time Start \_\_\_\_\_ Time finish \_\_\_\_\_ pledged \_\_\_\_\_

**[1]** An ideal 3 dimensional diatomic gas has the equation of state  $PV=nRT$  where  $n$  is the number of moles and  $R=8.314 \text{ J/(K mol)}$ . You may assume  $n=1$  mole here.

**(a)** Calculate  $c_p$  for this ideal gas when all 7 degrees of freedom are realized.

**For the rest of this problem, assume  $c_v=3/2 R$ .**

**(b)** Suppose  $n=1$  moles of this gas went through an isothermal process at  $T=300\text{K}$  which resulted in  $V_f=3V_i$  with  $V_i$  being the initial volume of the gas. Calculate the following quantities:

$$\Delta U = \underline{\hspace{2cm}}$$

$$Q = \underline{\hspace{2cm}}$$

**(c)** Suppose  $n=1$  moles of this gas went through an isobaric process at  $P=1.0 \times 10^2 \text{ Pa}$  and the volume changed from  $1 \text{ m}^3$  to  $3 \text{ m}^3$ . Calculate the following quantities:

$$\Delta T = \underline{\hspace{2cm}}$$

$$\Delta U = \underline{\hspace{2cm}}$$

$$Q = \underline{\hspace{2cm}}$$

**[2]** An unknown solid material is observed to have a length of 1 m at 0 °C and a length of 1.10 m at 100 °C.

**(a)** What is the coefficient of linear expansion for this material?

$\alpha =$  \_\_\_\_\_

**(b)** Another material (not the same material as in part a) has a coefficient of linear expansion given by  $\alpha = 2 \times 10^{-3} / ^\circ\text{C}$ . Calculate the coefficient of volume expansion for this material assuming the material is isotropic.

$\gamma =$  \_\_\_\_\_

**(c)** If a cube of the material in (b) above with a volume  $V_0 = 1 \text{ m}^3$  is heated from 0 °C to 100 °C, calculate the work done when it expands against a constant pressure of  $P = 1 \times 10^5 \text{ Pa}$ .

$W =$  \_\_\_\_\_

**(d)** Suppose the material in (b) above has a mass of 800 kg and a specific heat of  $c_p = 2 \text{ J}/(\text{kg } ^\circ\text{C})$ . Calculate the heat supplied to the system.

$Q =$  \_\_\_\_\_

**(e)** Calculate  $\Delta U$  when the material in (b) above is expanded (as in c) and simultaneously heated (as in d).

$\Delta U =$  \_\_\_\_\_

**(f)** Suppose a material has a specific heat that varies as  $c = c_0 T$  where  $c_0$  is a constant with SI units of  $\text{J}/(\text{kg } \text{K}^2)$  and  $T$  is temperature in Kelvin. If  $c_0 = 10 \text{ J}/(\text{kg } \text{K}^2)$ , find the heat required to change the temperature of 1 kg of this material from 200 K to 300 K.

$Q =$  \_\_\_\_\_

**[3]** A heat engine is reported to operate with 25 % efficiency when the cold reservoir is at  $0^{\circ}\text{C}$ .

**(a)** Assuming this engine follows the Carnot cycle, what is the temperature of the hot reservoir?

$T_H =$  \_\_\_\_\_

**(b)** Suppose the heat input to this engine was 10 J. Calculate the work done by this engine.

$W =$  \_\_\_\_\_

**(c)** Suppose the heat input to this engine was 5J. Calculate the heat rejected by this engine.

$Q_C =$  \_\_\_\_\_

**[4]** For water,  $\rho=1\times 10^3 \text{ kg/m}^3$ ,  $L_f=3.33\times 10^5 \text{ J/kg}$  and  $c=4186 \text{ J/Kg } ^\circ\text{C}$ .

**(a)** If 4 kg of water at  $0^\circ\text{C}$  is mixed with 1 kg of water at  $80^\circ\text{C}$ , calculate the final equilibrium temperature of the mixture.

$T_f=$  \_\_\_\_\_

**(b)** Calculate the change in entropy of the water as a result of the mixing described in part a. Hint: make sure your result is positive.

$\Delta S=$  \_\_\_\_\_

**(c)** If a 5 kg mass of ice at  $0^\circ\text{C}$  melts to become water at  $0^\circ\text{C}$ , calculate the change in entropy of the system.

$\Delta S=$  \_\_\_\_\_

**(d)** Suppose a ball of density  $\rho_b=8\times 10^2 \text{ kg/m}^3$  is floating in water. How much of the volume of the ball is below water?

$V_s=$  \_\_\_\_\_  $\text{m}^3$