

**Instructions: You have a total of 55 minutes to complete this test. Answer each of the following questions completely providing details and correct SI units.**

Time Start \_\_\_\_\_ Time finish \_\_\_\_\_ pledged \_\_\_\_\_

**[1]** An ideal 3 dimensional monotonic gas has the equation of state  $PV=nRT$  where  $n$  is the number of moles and  $R=8.314 \text{ J/(K mol)}$ . For this gas, it is known that the molar specific heat at constant volume is  $c_v= 3/2 R$ . You may assume  $n=1$  mole here.

**(a)** Calculate  $c_p$  and the adiabatic coefficient  $\gamma$  for this gas.

$C_p=$  \_\_\_\_\_  $\gamma=$  \_\_\_\_\_

**(b)** Suppose that the gas went through an **isobaric process ( $P=P_i$ )** which resulted in  $\Delta V=2V_i$  where  $V_i$  was the initial volume of the gas at the temperature  $T_i$  and pressure  $P_i$ . **In terms of  $P_i$  and  $V_i$** , calculate the following:

$Q=$  \_\_\_\_\_

$W=$  \_\_\_\_\_

$\Delta U=$  \_\_\_\_\_

**(c)** Suppose that the gas went through an **isothermal ( $T=T_i$ )** process which resulted in  $\Delta V=2V_i$  with  $P$  changing from  $P_i$  to  $P_f$ . Calculate the following **(in terms of the thermodynamic variable  $T_i$ )**:

$\Delta U=$  \_\_\_\_\_

$W=$  \_\_\_\_\_

$Q=$  \_\_\_\_\_

**[2]** An unknown solid material is observed to have a length of  $L_0=1$  m at  $0$  °C and a length of  $L=1.01$  m at  $100$  °C. **In your answers, be sure to use correct SI units.**

**(a)** Calculate the coefficient of linear expansion for this material.

$$\alpha = \underline{\hspace{2cm}}$$

**(b)** Another material (not the same material as in part a) has a coefficient of linear expansion given by  $\alpha=1 \times 10^{-3}$  /C. Calculate the coefficient of volume expansion for this material assuming the material is isotropic.

$$\gamma = \underline{\hspace{2cm}}$$

**(c)** If a cube of the material in (b) above with a volume  $V_0=1$  m<sup>3</sup> is heated from  $0$  °C to  $100$  °C, calculate the work done when it expands against a constant pressure of  $P=1 \times 10^5$  Pa.

$$W = \underline{\hspace{2cm}}$$

**(d)** Suppose the material in (b) above has a density of  $\rho=800$  kg/m<sup>3</sup> and a specific heat at a constant pressure of  $c_p=2$  J/(kg °C). Calculate the heat supplied to the system.

$$Q = \underline{\hspace{2cm}}$$

**(e)** Calculate  $\Delta U$  when the material in (b) above is expanded (as in c) and simultaneously heated (as in d).

$$\Delta U = \underline{\hspace{2cm}}$$

**[3]** A heat engine is reported to operate with 75% efficiency when the cold reservoir is at  $0^{\circ}\text{C}$ .

**(a)** Assuming this engine follows the Carnot cycle, what is the temperature of the hot reservoir (in K)?

$$T_H = \underline{\hspace{2cm}}$$

**(b)** Suppose the heat input to this engine was 50 J. Calculate the work done by this engine.

$$W = \underline{\hspace{2cm}}$$

**(c)** Suppose the heat input to this engine was 50J. Calculate the heat rejected by this engine.

$$Q_c = \underline{\hspace{2cm}}$$

**[4]** For water,  $L_f=3.33 \times 10^5$  J/kg and  $c=4186$  J/Kg  $^{\circ}\text{C}$ . **In your answers, be sure to use correct SI units.**

**(a)** If a 7 kg mass of ice at  $0^{\circ}\text{C}$  melts to become water at  $0^{\circ}\text{C}$ , calculate the change in entropy of the system.

$$\Delta S = \underline{\hspace{4cm}}$$

**(b)** If 7 kg of water at  $0^{\circ}\text{C}$  is mixed with 1 kg of water at  $50^{\circ}\text{C}$ , calculate the final equilibrium temperature of the mixture.

$$T_f = \underline{\hspace{4cm}}$$

**(c)** Calculate the change in entropy of the water as a result of the mixing described in part b. Your result is positive quantity.

$$\Delta S = \underline{\hspace{4cm}}$$