

(5) A rod of mass  $M$  and length  $L$  is attached to a wall as shown. A mass  $m$  is placed on the rod at a distance  $x$  from the wall. Find the tension in the cable, and the forces on the wall.

Steps:

(a) Choose the wall where the rod touches as the axis. The tension in the cable is  $T$ . Draw  $T_y$  and  $T_x$ , then write how  $T_y$  and  $T_x$  are related to  $T$  and the angle.

(b) The rod exerts forces on the wall. The wall exerts back Reactionary Forces denoted by  $R$ . Draw a vector indicating the direction of the reactionary forces.

(c) Indicate  $R_x$  and  $R_y$  by drawing these vectors which are acting on the rod.

(d) The conditions for static equilibrium are  $\sum \vec{F} = \vec{0}$  and  $\sum \vec{\Gamma} = \vec{0}$ . along the  $y$  direction, you have 4 components ( $R_y$ ,  $T_y$ ,  $Mg$  and  $mg$ ). Write the condition for  $F_y$  now.

(e) Along the  $x$ -direction you have 2 components ( $R_x$  and  $T_x$ ). Write the condition for  $F_x$  now.

(f) starting at the axis, walking across, you have 3 torques which are not zero. Apply the torque equation to find the sum of the torques.

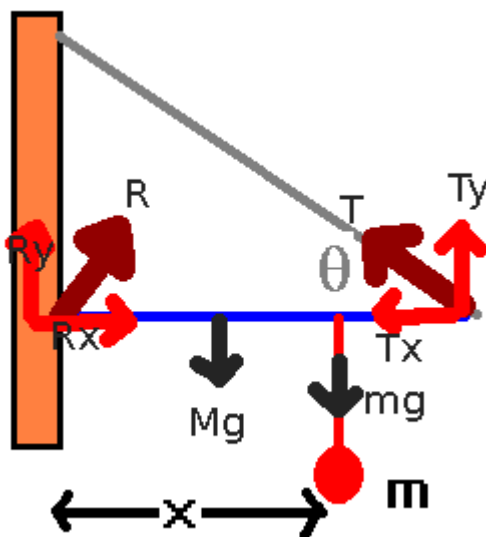
(g) Solve to the tension and the reactionary forces.

(a) Choose the wall where the rod touches as the axis. The tension in the cable is  $T$ . Draw  $T_y$  and  $T_x$ , then write how  $T_y$  and  $T_x$  are related to  $T$  and the angle.

$$T_x = T \cos \theta : T_y = T \sin \theta :$$

(b) The rod exerts forces on the wall. The wall exerts back Reactionary Forces denoted by  $R$ . Draw a vector indicating the direction of the reactionary forces.

(c) Indicate  $R_x$  and  $R_y$  by drawing these vectors which are acting on the rod.



(d) The conditions for static equilibrium are  $\sum \vec{F} = \vec{0}$  and  $\sum \vec{\Gamma} = \vec{0}$ . along the y direction, you have 4 components ( $R_y$ ,  $T_y$ ,  $Mg$  and  $mg$ ). Write the condition for  $F_y$  now.

$$\sum F_y = 0 \Rightarrow R_y - Mg - mg + T_y = 0 \quad (1)$$

(e) Along the x-direction you have 2 components ( $R_x$  and  $T_x$ ). Write the condition for  $F_x$  now.

$$\sum F_x = 0 \Rightarrow R_x - T_x = 0 \quad (2)$$

(f) starting at the axis, walking across, you have 3 torques which are not zero. Apply the torque equation to find the sum of the torques.

$$\sum \vec{\Gamma} = 0 \Rightarrow -\frac{MgL}{2} - mgx + T_y L = 0 \quad (3)$$

(g) Solve to the tension and the reactionary forces.

$$(3) \Rightarrow T_y = g \left( \frac{M}{2} - m \frac{x}{L} \right) = T \sin \theta \Rightarrow T = \frac{g \left( \frac{M}{2} - m \frac{x}{L} \right)}{\sin \theta} : T_x = T \cos \theta = \cot \theta g \left( \frac{M}{2} - m \frac{x}{L} \right) = R_x$$

$$(1) \Rightarrow R_y = Mg + mg - T_y = Mg + mg + g \left( \frac{M}{2} - m \frac{x}{L} \right)$$

$$R = \sqrt{R_x^2 + R_y^2}$$