

**Instructions: You have a total of 55 minutes to complete this test.**

**Answer each of the following questions completely.**

Time Start \_\_\_\_\_ Time finish \_\_\_\_\_ Pledged \_\_\_\_\_

**You must supply all details that led to your answer. You must provide correct SI units where required.**

**Do not discuss any aspect of this test with anyone until I return the test.**

(1) [a] A string has a mass attached to one end, thus forming a simple pendulum. It is observed that the pendulum has a period of  $T=5$  s. The same string is fully stretched between two poles and nailed at each end and tension is applied until a wave speed of 100 m/s is obtained. What is the frequency of the lowest lying mode of oscillation on the string?

[b] If a mass of 1 kg is attached to a spring, what would the spring constant need to be in order to produce a period of  $T=5$ s?

(2) A mass ( $m=5$  kg) is attached to a spring of spring constant  $k=250$  N/m. At  $t=0$ , the mass is moving through the equilibrium position with a speed of 10 m/s.

(a) What is then total energy of the system?

(b) What is the amplitude of oscillation?

(c) What is the period ( $T$ ) of the oscillation?

(3) Consider a closed organ pipe of length  $L=2.5$  m. Assuming that the speed of sound is 343 m/s, find the frequencies for the lowest lying 3 modes of oscillation.

(4) Suppose a sphere has a moment of inertia given by  $I = \frac{1}{3}mR^2$  about an axis through its center of mass. A force  $F = bt$  is applied tangent to the sphere which is initially at rest. After a time  $t$ , find the following:

(a) what is the angular acceleration in terms of  $m$ ,  $R$ ,  $b$  and  $t$ ?

(b) what is the angular velocity in terms of  $m$ ,  $R$ ,  $b$  and  $t$ ?

(c) what is the kinetic energy in terms of  $m$ ,  $R$ ,  $b$  and  $t$ ?

(d) what is its angular momentum in terms of  $R$ ,  $b$ ,  $c$  and  $t$ ?